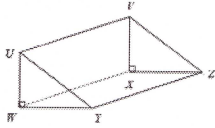


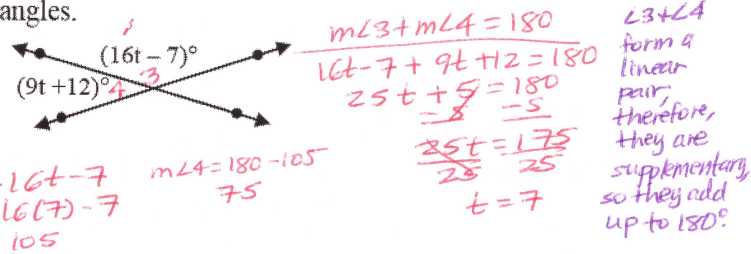
1) In the figure below, points W, X, Y, and Z lie on plane WXY. State the postulate that can be used to show that the statement below is true.

X and Y are collinear.



- If two lines intersect, then their intersection is exactly one point.
- A line contains at least two points. *Since only two points are involved, this is not the answer.*
- If two points lie in a plane, then the entire line containing those points lies in that plane.
- Through any two points there is exactly one line.

5) The runways at an airport intersect as shown. The measure of $\angle 3$ at the intersection is $(16t - 7)^\circ$ and the measure of $\angle 4$ is $(9t + 12)^\circ$. Find the measure of both angles.



m∠3: 105 m∠4: 75

In #2-4, find the measure of each numbered angle.

2) $m\angle 13 = 4x + 11$; $m\angle 14 = 3x + 1$

L3+L14 form a linear pair, they are, therefore, supplementary (i.e., they add up to 180°)

$m\angle 13 + m\angle 14 = 180$
 $4x + 11 + 3x + 1 = 180$
 $7x + 12 = 180$
 $7x = 168$
 $x = 24$

$m\angle 13 = 4(24) + 11 = 96 + 11 = 107$
 $m\angle 14 = 3(24) + 1 = 72 + 1 = 73$

you can also plug x into both expressions + simplify

m∠13: 107 m∠14: 73

3) $m\angle 4 = 3x - 8$; $m\angle 5 = 7x - 12$

L3 is a right L, so L4+L5 form a right L; therefore, they add up to 90°

$m\angle 4 + m\angle 5 = 90$
 $3x - 8 + 7x - 12 = 90$
 $10x - 20 = 90$
 $10x = 110$
 $x = 11$

$m\angle 4 = 3(11) - 8 = 33 - 8 = 25$
 $m\angle 5 = 7(11) - 12 = 77 - 12 = 65$

Since this angle is a right angle, L3 is also a right L since they form a linear pair

you can also plug x into both expressions and simplify

m∠3: 90 m∠4: 25 m∠5: 65

4) $m\angle 2 = 4x - 26$; $m\angle 3 = 3x + 4$

L2+L3 are vertical Ls, therefore they are congruent, so they have the same measure; therefore, they are equal to each other.

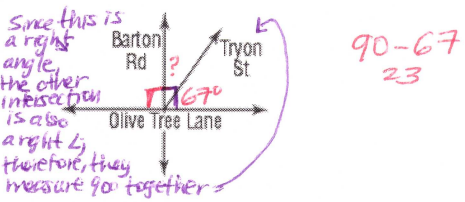
$m\angle 2 = m\angle 3$
 $4x - 26 = 3x + 4$
 $x - 26 = 4$
 $x = 30$

$m\angle 2 = 4(30) - 26 = 120 - 26 = 94$
 $m\angle 3 = 3(30) + 4 = 90 + 4 = 94$

Since these are congruent, you only need to find one of the measures; it doesn't matter which one.

m∠2: 94 m∠3: 94

6) Refer to the figure below. Barton Road and Olive Tree Lane form a right angle at their intersection. Tryon Street forms a 67° angle with Olive Tree Lane. What is the measure of the acute angle Tryon Street forms with Barton Road?



7) The figure to the right shows the intersection of two tracks at a junction.



A) Are the angles at the intersection given by $\angle 1$ and $\angle 2$ congruent? Yes

B) How do you know? $\angle 1$ and $\angle 2$ are vertical Ls.

8) Determine whether the following statements are always, sometimes, or never true.

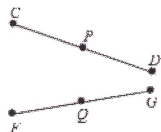
- Two angles that are complementary are supplementary. Never
The opposite (the converse) is never true either.
- Supplementary angles are congruent. sometimes
This would work if they are both right angles.

9) Use the reasons and statements bank below to complete the proof that follows. There is an extra option.

CP=PD	Definition of \cong segments	Substitution	Substitution
$\overline{PD} \cong \overline{QG}$	Segment Addition Postulate	Definition of \cong segments	FQ=QG

Given: $\overline{CP} \cong \overline{FQ}$; P is the midpoint of \overline{CD} ; Q is the midpoint of \overline{FG} .

Prove: $\overline{PD} \cong \overline{QG}$

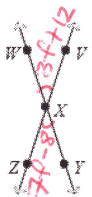


Statements	Reasons
1. $\overline{CP} \cong \overline{FQ}$ P is the midpoint of \overline{CD} Q is the midpoint of \overline{FG} .	1. Given
2. $CP=FQ$	2. Def. of \cong segments
3. $CP=PD$ <i>any other is fine</i> $FQ=QG$	3. Definition of midpoint
4. $PD=FQ$	4. Substitution
5. $PD=QG$	5. Substitution
6. $\overline{PD} \cong \overline{QG}$	6. Def. of \cong segments

10) \overline{WY} and \overline{VZ} intersect at point X, $m\angle WXV = 3f + 12$, and $m\angle ZXY = 7f - 8$. Prove $f=5$.

$$\begin{array}{r} 3f+12 = 7f-8 \\ -3f \quad -3f \\ \hline -4f+12 = -8 \\ -12 \quad -12 \\ \hline -4f = -20 \\ \div -4 \quad \div -4 \\ \hline f = 5 \end{array}$$

$$\begin{array}{r} 3f+12 = 7f-8 \\ -3f \quad -3f \\ \hline 12 = 4f-8 \\ +8 \quad +8 \\ \hline 20 = 4f \\ \div 4 \quad \div 4 \\ \hline 5 = f \end{array}$$



Statements	Reasons
1. $\angle WXV$ and $\angle ZXY$ are vertical angles	1. Definition of vertical angles
2. $\angle WXV \cong \angle ZXY$	2. Vertical \angle theorem
3. $m\angle WXV = m\angle ZXY$	3. Definition of congruency
4. $m\angle WXV = 3f + 12$, and $m\angle ZXY = 7f - 8$	4. Given
5. $3f + 12 = 7f - 8$	5. Substitution Prop. Of Equality
6. $-4f + 12 = -8$	6. Subtraction Prop
7. $-4f = -20$	7. Subtraction Prop
8. $f = 5$	8. Division Prop.

Alternate answer:

- 6) $12 = 4f - 8$ Subtraction Prop.
- 7) $20 = 4f$ Addition Prop.
- 8) $5 = f$ Division Prop.
- 9) $f = 5$ Symmetric Prop.

11) If $AB = 2BC$, then $AC = 3BC$.



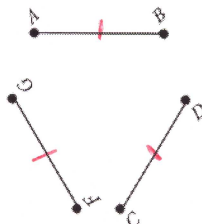
Statements	Reasons
1. $AB = 2BC$	1. Given
2. $AC = AB + BC$	2. Segment Addition Postulate
3. $AC = 2BC + BC$	3. Substitution
4. $AC = 3BC$	4. substitution/simplify

12) Write a two-column proof:
If $12h - 6 = 30$, then $h = 3$

$$\begin{array}{r} 12h - 6 = 30 \\ +6 \quad +6 \\ \hline 12h = 36 \\ \div 12 \quad \div 12 \\ \hline h = 3 \end{array}$$

Statements	Reasons
1) $12h - 6 = 30$	1) Given
2) $12h = 36$	2) Addition Property
3) $h = 3$	3) Division Property

13) Write a two-column proof.
If $\overline{AB} \cong \overline{DC}$ and $\overline{DC} \cong \overline{FG}$ then $\overline{AB} \cong \overline{FG}$.



Statements	Reasons
1) $\overline{AB} \cong \overline{DC}$ <i>1st</i> $\overline{DC} \cong \overline{FG}$ <i>2nd</i>	1) Given
2) $\overline{AB} \cong \overline{FG}$ <i>1st</i> $\overline{DC} \cong \overline{FG}$ <i>3rd</i>	2) Transitive Property